YFAR 10 — DEVELOPING ALGEBRA Representing solutions of equations and

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YFAR 10 - DEVELOPING ALGEBRA Simultaneous Equations

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YFAR 10 - SIMILARITY

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Congruence, similarity & enlargement

What do I need to be able to do?

By the end of this unit you should be able to:

- Enlarge by a positive scale factor
- Enlarge by a fractional scale factor
- Identify similar shapes
- Work out missing sides and angles in similar shapes
- Use parallel lines to find missing angles
- Understand similarity and congruence

Keywords

- Enlarge: to make a shape bigger (or smaller) by a given multiplier (scale factor)
- Scale Factor: the multiplier of enlargement
- Centre of enlargement: the point the shape is enlarged from
- Similar: when one shape can become another with a reflection, rotation, enlargement or translation. Congruent: the same size and shape
 - Corresponding: items that appear in the same place in two similar situations

Parallel: straight lines that never meet (equal gradients)



YEAR 10 - SIMILARITY ...

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Trigonometry



YEAR 10 - PROPORTION ...

Ratios and fractions

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Keywords What do I need to be able to do? Ratio: a statement of how two numbers compare By the end of this unit you should be able to: Equivalent: of equal value Compare quantities using ratio Link ratios and fractions and make Proportion: a statement that links two ratios comparisons Integer: whole number, can be positive, negative or zero. Share in a given ratio Fraction: represents how many parts of a whole. Link Ratio and scales and graphs Denominator: the number below the line on a fraction. The number represent the total number of parts. Solve problems with currency conversions Numerator: the number above the line on a fraction. The top number. Represents how many parts are taken Solve 'best buy' problems Origin: (0,0) on a graph. The point the two axes cross Combine ratios Gradient: The steepness of a line Ratios and fraction R Sharing a whole into a given Compare with ratio \, 🔃 "For every dog there are 2 cats" Trees ratio James and Lucy share £350 in the Trees: Flowers ratio 3:4 Ratic Dogs: Cats 🔊 3:7 Work out how much each person earns Units have 12 the be of Model the Question James the same Flowers The ratio has to be written in the James: Lucy Fraction of trees value to same order as the information is 3:4 compare Fraction given Number of parts of in group 3 ratios e.g. 2:1 would represent 2 dogs for Total number of parts Lucy everu I cat Find the value of one part £350 + 7 = £50 Whok: £.350 Ratio and scale Ratio and graphs 🔃 7 parts to share between = one part Ц (3 James, 4 Lucu) £50 Graphs with a constant ratio are П Q picture of a car is drawn with a scale of 1:30 Put back into the question directly proportional П James = 3 x £50 = £ 150 Form a straight line П James: Lucy Pass through (0,0) The car image is Ш x 50 3:4 x 50 10cm П Image : Real life ▲ £ 150:£200 П lcm : 30cm The gradient is the constant ratio 10cm : 300cm Lucy = 4 x £50 = £200 Ratios in I:n and n:1 This is asking you to cancel down Conversion between currencies until the part indicated represents 1. £1 = 90 Rupees Currency is directly proportional Show the ratio 4:20 in the ratio of In For every £1 £1 = 90 Rupees I have 90 Rupees The question states 4:20· This side has to that **this part has to** f. 10 = 900 Rupees be divided by 4 be l'unit. Currency can be converted too — to keep in Therefore proportion using a conversion graph Divide by 4 goop goop Convert 630 Rupees into Pounds the n part does not have to be an integer for this type of questio = 90 Rupees Combining ratios G 10 Pounds = 630 Rupees The ratio of Blue counters to Red counters is 5:3 The ratio of Red counters to Green counters is 2:1 0 Best buus You could work out how much 40 pens are and 0.0 then compare Ratio of Blue to Red to Green Compare the solution in the context of the question 3 4 pens costs £2.60 10 pens costs £6.00 10 6 The best value has the "I pen Use equivalent ratios to allow $£260 \div 4 = £0.65$ $\pounds 6.00 \div 10 = \pounds 0.60$ lowest cost "per pen" costs... Lowest common multiple of comparison of the group that is The best value means £1 the ratio both statements "I-pound common to both statements $10 \div 6 = 1.67 \text{ pens}$ 4 ÷ 2.60 = 154 pens buys you more pens share. buus...

YEAR 10 - PROPORTION.

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Percentages and Interest



YEAR 10 - PROPORTION ...

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Keywords What do I need to be able to do? Event: one or more outcomes from an experiment By the end of this unit you should be able to: Odd, Subtract and multiply fractions Outcome: the result of an experiment. Find probabilities using likely outcomes Intersection: elements (parts) that are common to both sets Use probability that sums to 1 Union: the combination of elements in two sets. Estimate probabilities Expected Value: the value/ outcome that a prediction would suggest you will get Use Venn diagrams and frequency trees Universal Set: the set that has all the elements Use sample space diagrams Sustematic: ordering values or outcomes with a strategy and sequence Calculate probability for independent events Product: the answer when two or more values are multiplied together. Use tree diagrams Likeliness of a probability Odd, Subtract and multiply fractions R

Probability



YEAR 10 - GEOMETRY...

therefore are the

same, size.

Angles and bearings @whisto maths Keywords What do I need to be able to do? By the end of this unit you should be able Cardinal directions: the directions of North, South, East, West to: Ongle: the amount of turn between two lines around their common point Understand and represent bearings Bearing: the angle in degrees measured clockwise from North. Measure and read bearings Perpendicular: where two lines meet at 90° Make scale drawings using bearings Parallel: straight lines always the same distance apart and never touch. They have the same gradient. Calculate bearings using angle rules Clockwise: moving in the direction of the hands on a clock. Solve bearings problems using Construct: to draw accurately using a compass, protractor and or ruler or straight edge. Pythagoras and trigonometry Scale: the ratio of the length of a drawing to the length of the real thing. Protractor: an instrument used in measuring or drawing angles Draw angles up to 180° Measure angles to 180° Ongle notation The letter in the middle is the angle The site and bene measured The arc represents the part of the angle Draw a 35° angle Make a mark at 35° with a pencil Read from 0° on Ond join to the angle point (use a the base line. nule.r) Remember to use estimation. This is an obtuse angle Ongle Notation: three letters $A\widehat{B}C$ This is the angle at so between 90 ° B = 113 ° and 180 ° ∠ABC is also used to represent the angle at B. 1ake sure the cross Make sure the cross is at the end Scale drawings The base line follows is at the point the of the line (where you want the The anale the line segment two lines meet angle) 1:20 For every Icm on the model there are 20cm in real life Inderstand and represent bearings The angle indicated starts from the North line at Q and joins the path connecting Q to B. Q bearing is always measured Remember: Scale drawings ONLY change lengths and distances. from NORTH Onales remain the same This angle shows the bearing of **B from** A It is always given as three figures Directions The bearing of B from Q is The sentence... "Bearing of . from calculated by measuring the really important in identifying the bearing being highlighted angle represented Using estimation it is clear this angle is between 090° and 180° Onti-Clockwise Clockwise Scale drawings using bearings Measure and read bearings Remember — angles <mark>DO NOT</mark> change size in scaled drawings The bearing of the cow to the barn. This angle is measured from NORTH The bearing measurements do not change from "real life" It is measured in a clockwise direction to images Estimation indicates this angle is between 180° and 270° The units in the ratio Use a protractor to measure accurately scale are the same Remember: bearings are written as three figures. 6 cm = 30 kmThe scale may need to be calculated from the image The auxiliary line is drawn to help you measure and draw 6:3,000,000 This represents 30km from P to Q. 🗲 the angle that is measured to represent the bearing. ______ _____ _____ Bearings with right-angled geometru Bearings with angle rules Look for Right-angles: Because two North Ines are POROLLEL... Pythagoras "Due West" "Due, Fast Trigonometry (Sin, Cos, Tan, bearing of 090° bearing of 270° makes a 90° makes a 90° 110° 110° Don't forget the 90° here too 110° angle angle 20km They form h Q plane flies East for 20km 15km corresponding h They form **alternate** then turns South for 15km Use $\tan^{-1}\left(\frac{15}{20}\right)$ to calculate They form <u>co-interior</u> angles and angles and therefore are Find the bearing of the plane Ц angles and add up to

the same size

h

180°

this angle

from where it took off.

YFAR 10 - GEOMETRY

surface area

of a sphere

Working with circles

trianale

@whisto maths Keywords What do I need to be able to do? By the end of this unit you should be able Circumference: the length around the outside of the circle - the perimeter to: Orea: the size of the 2D surface Recognise and label parts of a circle Diameter: the distance from one side of a circle to another through the centre Calculate fractional parts of a circle Radius: the distance from the centre to the circumference of the circle Calculate the length of an arc Tangent: a straight line that touches the circumference of a circle Calculate the area of a sector Chord: a line segment connecting two points on the curve Understand and use volume of a cone. Frustrum: a pyramid or cone with the top cut off cylinder and sphere. Hemisphere: half a sphere Understand and use surface area of a Surface area: the total area of the surface of a 3D shape. cone, culinder and sphere. Parts of a circle Fractional parts of a circle a circle is made up of 360° R Formula to remember: Sector (part of Orea of a circle = πr^2 the circle made 🛽 30° represents $\frac{30}{360}$ of a full circle Circumference of a circle = πd or $2\pi r$ from two radii) $\frac{30}{360} = \frac{1}{12}$ The fraction of the circle is as $\frac{\theta}{360}$ Segment (part chord 270 360 of a full circle (in degrees) of the circle $\frac{3}{4}$ of a full circle made from a heta represents the degrees in the $\frac{6}{2}$ of a full circle (in equal parts) chord) sector Circumference On arc is a part of the circumfe.re.nce. Remember a sector is part of a circle • Orea of the whole circle = $\pi r^2 = \pi \times 6^2 = 36\pi$ Remember an arc is part of the circumference Sector area Orc length Circumference of the whole circle = πd = $\pi \times 9 = 9\pi$ $=\frac{120}{360}\times 36\pi$ $=\frac{240}{360}\times 9\pi$ 240; 1209 $\frac{\theta}{2}$ × area of circle. Sector area $\text{Orc length} = \frac{\theta}{360} \times \text{circumference}$ $=\frac{2}{2} \times 9\pi = 6\pi$ $=\frac{1}{2} \times 36\pi = 12\pi$ Perimeter Perimeter is the length ground the outside of the shape Volume of a cone and a cylinder This includes the arc length and the radii that encloses the shape Perimeter = $\frac{\theta}{360}$ × circumference + 2r $= 6\pi + 9$ Volume Cylinder= $\pi r^2 h$ Volume Cone = $\frac{1}{2}\pi r^2 h$ O culinder is a prism - cross section is a circle Q cone is a pyramid with a circular base Volume of a sphere Volume Sphere = $\frac{4}{3}\pi r^3$ $V = \pi r^2 h$ The height of a cone is NOTE: This is now a cubed value the perpendicular height Volume Sphere = $\frac{4}{2}\pi r^3$ $= \pi \times 42 \times 10$ from the vertex to the 10cm $= \pi \times 160$ $\frac{4}{2} \times \pi \times 3^3$ Look out for hase hemispheres being $= 160\pi$ cm² $=\frac{4}{2} \times \pi \times 27 = 36\pi$ placed on other 3D Look out for trigonometry or shapes, e.g. cones and Give your answer in terms of π' a hemisphere is half = $36\pi \div 2$ Pythagoras theorem — the radius culinders 502.7cm² means **NOT** in terms of pi the volume of the forms the base of a right-angled *-* 18π overall sphere Surface area of a sphere Surface area of cones and culinders Surface area = $4\pi r^2$ Surface area cylinder= $2\pi r^2 + \pi dh$ Radius = 5cm Curved surface area Cone = $\pi r l$ Q hemisphere has the curved surface QND a flat circular Look out for the use of Pythagoras to Surface area = $4\pi r^2$ face R calculate the length l $= 4 \times \pi \times 5^2$ The area of two circles (top and bottom face) + the area Total surface area = $= 4 \times \pi \times 25$ $= 100\pi \div 2 = 50\pi$ of the curved face curved face + circle face (area of base) The curved 100π - $= 50\pi + \pi \times 5^2$

The length of shape B is the circumference of the circles

Hemisphere $= 75\pi$

YFAR 10 - GEOMETRY...

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needs a scalar of -1

YFAR 10 — DFIVING INTO DATA Collecting, representing and interpreting

@whisto maths

What do I need to be able to do?

By the end of this unit you should be able to:

- Construct and interpret frequency tables and polygon. two-way tables, line, bar, & pie 1 charts
- Find and interpret averages from a list and a table
- Construct and interpret time series graphs, stem and leaf diagrams and scatter araphs

<u>Keywords</u>

Population: the whole group that is being studied Sample: a selection taken from the population that will let you find out information about the larger group Representative: a sample group that accurately represents the population

Random sample: a group completely chosen by change. No predictability to who it will include.

Bias: a built-in error that makes all values wrong by a certain amount

Primary data: data collected from an original source for a purpose.

Secondary data: data taken from an external location. Not collected directly.

Outlier: a value that stands apart from the data set



The data in a list: 45, 55, 55, 55, 65, 65, 65, 65, 65

10 — DELVING INTO DATA Collecting, representing and interpreting @whisto maths

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YEAR 10 - USING NUMBER...

Non-calculator methods

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YEAR 10 - USING NUMBER...

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Types of number & sequences



<u>Keywords</u>



YFAR 10 — USING NUMBER

 $2^{-2} = \frac{1}{4}$

Indices & Roots @whisto maths Keywords What do I need to be able to do? By the end of this unit you should be able to: Standard (index) Form: A system of writing very big or very small numbers Identify square and cube numbers Commutative: an operation is commutative if changing the order does not change the result Calculate higher powers and roots Base: The number that gets multiplied by a power Understand powers of 10 and standard **Power**: The exponent — or the number that tells you how many times to use the number in multiplication form Exponent: The power — or the number that tells you how many times to use the number in multiplication Know the addition and subtraction rule for Indices: The power or the exponent. indices Negative: a value below zero. Understand power zero and negative Coefficient: The number used to multiply a variable indices Calculate with numbers in standard form I Higher powers and roots Cube numbers Square and cube numbers 144 216 Square numbers - DOWRY (number of times I. 4, 9, IG. . . 1, 8, 27, 64, 125... multiplied by 36 itself) 2 the, base, 144 = 2x2x2x2x3x3 **216**=2x2x2x3x3x3 number 2 2x2x3x2x2x311 2 x 3 x 2 x 3 x 2 x 3 12 x 12 6 x 6 x 6 $\sqrt[n]{x}$ Finding the *n*th Prime factors can find square root root of any value $\sqrt[3]{216} = 6$ $\sqrt{144} = 12$ 3 <u>Other mental strategies for square roots</u> Standard form R $\sqrt{810000} = \sqrt{81} \times \sqrt{10000}$ Ony integer 0.001 100 10 1000 $= 9 \times 100$ Onu number $|\chi|^{\frac{1}{1000}}$ 10-2 101 100 10-1 10-3 10^{n} $A \times$ between I and = 900less than 10 1 x 10-3 Negative powers do not Oddition/ Subtraction Laws Ony value to the power O always = 1 Example Non-example indicate negative solutions 3.2 x 10 4 0.8 x 10 4 Numbers in standard form with negative $a^m X a^n = a^{m+n}$ = 3.2 x 10 x 10 x 10 x 10 powers will be less than 1 5.3 x 10⁽⁰⁷⁾ - 32000 $3.2 \times 10^{-4} = 32 \times \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} = 0.00032$ $a^m \div a^n = a^{m-n}$ Standard form calculations Powers of powers Zero and negative indices Addition and Subtraction Tip: Convert into ordinary numbers $x^0 = 1$ $(x^a)^b = x^{ab}$ first and back to standard from at the end $6 \times 10^5 + 8 \times 10^5$ Method 2 Method I $\frac{a^6}{a^6} = a^6 \div a^6$ $(2^3)^4 = 2^3 \times 2^3 \times 2^3 \times 2^3$ = (6 + 8) x 10⁵ = 600000 + 800000 any number 14 x 10⁵ divided by The same base and power is repeated. Use the addition = 1400000 This is not the 1.4 x 10¹ x 10⁵ itself = 1 law for indices = 1.4 x 10⁵ final answer $=a^{6-6}=a^0=1$ <u>= 1.4 x 105</u> $(2^3)^4 = 2^{12}$ $-a \times b = 3x4 = 12$ Multiplication and division Negative indices do not indicate Division questions NOTICE the difference negative solutions 1.5 x 10⁵ can look like this $2^2 = 4$ $(2x^3)^4 = 2x^3 \times 2x^3 \times 2x^3 \times 2x^3$ 0.3×10^3 For multiplication × $2^1 = 2$ and division you $2^0 = 1$ (1.5)x 10⁵)÷ Looking at the sequence (0.3) x 10³) can look at the The addition law applies ONLY to the powers. can help to understand values for A and $2^{-1} = \frac{1}{2}$ The integers still need to be multiplied negative powers $1.5 \div 0.3$ x $10^{5} \div 10^{3}$ the powers of 10 as two separate $(2x^3)^4 = 16x^{12}$

calculations

= 5 x 10²